#### 6<sup>th</sup> GECCO Workshop on Blackbox Optimization Benchmarking (BBOB): Turbo Intro to COCO/BBOB

#### The **BBOBies**

https://github.com/numbbo/coco



slides based on previous ones by A. Auger, N. Hansen, and D. Brockhoff

### **Numerical Blackbox Optimization**

#### Optimize $f: \Omega \subset \mathbb{R}^n \mapsto \mathbb{R}^k$



#### derivatives not available or not useful

### **Practical Blackbox Optimization**



#### Not clear:

which of the many algorithms should I use on my problem?

### **Need: Benchmarking**

- understanding of algorithms
- algorithm selection
- putting algorithms to a standardized test
  - simplify judgement
  - simplify comparison
  - regression test under algorithm changes

#### Kind of everybody has to do it (and it is tedious):

- choosing (and implementing) problems, performance measures, visualization, stat. tests, ...
- running a set of algorithms

## that's where COCO and BBOB come into play Comparing Continuous Optimizers Platform https://github.com/numbbo/coco

#### automatized benchmarking

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#### example\_experiment.c





/coco/issues.

#### result folder

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#### automatically generated results



#### automatically generated results



### **Measuring Performance**

#### On

- real world problems
  - expensive
  - comparison typically limited to certain domains
  - experts have limited interest to publish
- "artificial" benchmark functions
  - cheap
  - controlled
  - data acquisition is comparatively easy
  - problem of representativeness

COCO/BBOB

### **Test Functions**

define the "scientific question"

the relevance can hardly be overestimated

- should represent "reality"
- are often too simple?

remind separability

account for invariance properties

prediction of performance is based on "similarity", ideally equivalence classes of functions

### **Available Test Suites in COCO**

- bbob
- bbob-noisy
- bbob-biobj

24 noiseless fcts

- 30 noisy fcts
- 55 bi-objective fcts

140+ algo data sets

40+ algo data sets new < in 2016 15 algo data sets

### **How Do We Measure Performance?**

Meaningful quantitative measure

- quantitative on the ratio scale (highest possible)
  - "algo A is two times better than algo B" is a meaningful statement
- assume a wide range of values
- meaningful (interpretable) with regard to the real world possible to transfer from benchmarking to real world

runtime or first hitting time is the prime candidate (we don't have many choices anyway)

### **How Do We Measure Performance?**

**Two objectives:** 

- Find solution with small(est possible) function/indicator value
- With the least possible search costs (number of function evaluations)

For measuring performance: fix one and measure the other

### **Measuring Performance Empirically**



number of function evaluations

#### ECDF:

## Empirical Cumulative Distribution Function of the Runtime [aka data profile]

### 15 Runs



### **15 Runs ≤ 15 Runtime Data Points**



### **Empirical Cumulative Distribution**



the ECDF of run lengths to reach the target

- has for each
   data point a
   vertical step of
   constant size
- displays for each x-value (budget) the count of observations to the left (first hitting times)

e.g. 60% of the runs need between 2000 and 4000 evaluations 80% of the runs reached the target



15 runs



#### 15 runs 50 targets



15 runs 50 targets



15 runs 50 targets ECDF with 750 steps



#### 50 targets from 15 runs

...integrated in a single graph

### **Fixed-target: Measuring Runtime**



### **Fixed-target: Measuring Runtime**

• Algo Restart A:



• Algo Restart B:

 $-RT_B^r$   $p_s(Algo Restart A) = 1$ 

### **Fixed-target: Measuring Runtime**

• Expected running time of the restarted algorithm:

$$E[RT^{r}] = \frac{1 - p_{s}}{p_{s}} E[RT_{unsuccessful}] + E[RT_{successful}]$$

• Estimator average running time (aRT):

$$\widehat{p_s} = \frac{\# \text{successes}}{\# \text{runs}}$$

 $\widehat{RT_{unsucc}}$  = Average evals of unsuccessful runs

 $\widehat{RT_{succ}}$  = Average evals of successful runs

$$aRT = \frac{\text{total #evals}}{\text{#successes}}$$

### **ECDFs with Simulated Restarts**

What we typically plot are ECDFs of the simulated restarted algorithms:



### Worth to Note: ECDFs in COCO

In COCO, ECDF graphs

- never aggregate over dimension
  - but often over targets and functions
- can show data of more than 1 algorithm at a time

# the recent extension to multi-objective optimization

### bbob-biobj Testbed (new in 2016)

- 55 functions, combining bbob functions
- 6 dimensions (2..40D)
- no normalization
- ideal/nadir known
- but Pareto set/front no

1 Separable Functions				4 M	lulti-n	nodal	functi	ons w	ith ad	equat	e glob	al stri	ucture
f1	Sphere Function 🗸			f15									
f2	Sellipsoidal Function 🗸			f16	Weierstrass Function								
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f4	Büche-Rastrigin Function			f18	So	Schaffers F7 Functions, moderately ill-conditioned							
f5	Linear Slope			f19	Co	mpos	ite Gri	ewank	-Rose	nbroc	k Func	tion F8	3F2
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not (only refsets) $f_{17}$										<u>f46</u>	<u>f47</u>	<u>f48</u>	<u>f49</u>
											<u>f50</u>	<u>f51</u>	<u>f52</u>
												<u>f53</u>	<u>f54</u>

 $f_{21}$ 

f55

### **Bi-objective Performance Assessment**

algorithm quality =

normalized\* hypervolume (HV) of all non-dominated solutions

if a point dominates nadir

closest normalized\* negative distance to region of interest [0,1]<sup>2</sup>

if no point dominates nadir

\* such that ideal=[0,0] and nadir=[1,1]



### **Bi-objective Performance Assessment**

We measure runtimes to reach (HV indicator) targets:

- relative to a reference set, given as the best Pareto front approximation known (since exact Pareto set not known)
  - for the workshop: before\_workshop values
  - from now on: updated current\_best values incl. all nondominated points found by the 15 workshop algos: will be available soon and hopefully fixed for some time
- actual absolute hypervolume targets used are

HV(refset) – targetprecision

with 58 fixed targetprecisions between 1 and -10<sup>-4</sup> (same for all functions, dimensions, and instances) in the displays

### **BBOB-2016 Session II**

10:40 - 10:55	The BBOBies: Session Introduction
10:55 - 11:20	Cheryl Wong*, Abdullah Al-Dujaili, and Suresh Sundaram: Hypervolume-based DIRECT for Multi-Objective Optimisation
11:20 - 11:45	Abdullah Al-Dujaili* and Suresh Sundaram: A MATLAB Toolbox for Surrogate-Assisted Multi-Objective Optimization: A Preliminary Study
11:45 - 12:10	Oswin Krause*, Tobias Glasmachers, Nikolaus Hansen, and Christian Igel: Unbounded Population MO-CMA-ES for the Bi-Objective BBOB Test Suite
12:10 - 12:30	The BBOBies: Session Wrap-up

#### http://coco.gforge.inria.fr/

